THEORY OF ELLIPTIC CURVES AND ITS APPLICALTIONS I

1	Course Title:	THEORY OF ELLIPTIC CURVES AND ITS APPLICALTIONS I	
2	Course Code:	MAT6111	
3	Type of Course:	Optional	
4	Level of Course:	Third Cycle	
5	Year of Study:	1	
6	Semester:	1	
7	ECTS Credits Allocated:	5.00	
8	Theoretical (hour/week):	3.00	
9	Practice (hour/week):	0.00	
10	Laboratory (hour/week):	0	
11	Prerequisites:	none	
12	Language:	Turkish	
13	Mode of Delivery:	Face to face	
14	Course Coordinator:	Prof. Dr. İSMAİL NACİ CANGÜL	
15	Course Lecturers:	Prof. Dr. Osman Bizim	
16	Contact information of the Course Coordinator:	Uludağ Üniversitesi, Fen-Edebiyat Fakültesi Matematik Bölümü, Görükle Bursa-TÜRKİYE 0 224 294 17 57 / obizim@uludag.edu.tr	
17	Website:		
18	Objective of the Course:	The theory of elliptic curves brings important areas of mathematics such as abstract algebra, number theory and related fields. The aim of this course is to make the students get all connections among all these areas. The goal is to teach the elementary theory of elliptic curves. So students can bring new ideas the theory of elliptic curves and have the ability conduct original research and independent publication.	
19	Contribution of the Course to Professional Development:		
20	Learning Outcomes:		
		1	Learn the group structure of the points on the elliptic curves and the proof of associativity.
		2	Learn division polynomials and torsion points of the elliptic curves and Weil pairing and Tate-Licthenbaum pairing.
		3	Learn elliptic curves over finite fields and counts the number of the points on these curves, the theorem of Hasse, Frobenius enomorphism an Schoof's algorithm.
		4	Learn the discrete logarithm problem, general attacks on discerete logs, baby step, giant step, Pollard's method, the Pohling-Hellman method.
		5	Learn MOV attack, Frey-Rück attack and other attacks.
		6	Learn the elliptic curves over Q and the torsion subgroup and the Lutz-Nagell theorem, the method of descent, the Mordell- Weil theorem.
		7	Learn the elliptic curves over C, doubly periodic functions, tori are elliptic curves, the arithmetic and geometric mean. Cantor's algorithm, zeta functions, Fermat's last theorem, sketch of Wiles's proof.

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21	Course Content:

Course Content:

Week	Theoretical	Practice
1	Basic concepts of elliptic curves, the group law on the elliptic curves and proof of associativity.	
2	Other equations for elliptic curves, Legendre equation, cubic equations and quartic equations. The j-invariant of an elliptic curve and isomorphisms and endomorphisms of the curves.	
3	Torsion points of elliptic curves and division polynomials of an elliptic curve. Weil paring, Tate-Licthenbaum pairing.	
4	Elliptic curves over finite fields, counting the number of the points on these curves and the theorem of Hasse, The frobenius endomorphism, Schoof's Algorithm.	
5	Determining the group structure of the points on the elliptic curves over finite fields and the group order. Some family of elliptic curves over finite fields, singular and supersingular curves.	
6	MOV attack, Frey-Rück attack and other method.	
7	The basic concepts in the elliptic curve cryptography, Massey-Omura encryption.	
8	ElGamal public key encryption and the digital signature algorithm.	
9	The elliptic curves over Q and the torsion subgroup and the Lutz-Nagell theorem, the theorem.	
10	Mordell-Shafarevich-Tate groups, Galois cohomology.	
11	Elliptic curves over C, lattices and elliptic functions, tori are elliptic curves, the arithmetic and geometric mean.	
13	Division poliynomials and the torsion subgroups, Doud's method, complex multiplication and numerical examples, the integrality of j-invariants.	
14	Hyperelliptic curves, Cantor's algorithm, zeta functions, Fermat's last theorem, sketch of Wiles's proof.	

Activites	Number	Duration (hour)	Total Work Load (hour)
Theoretical	14	3.00	42.00
Practicals/Labs	0	0.00	0.00
Self study and preperation	14	5.00	70.00
Homeworks	0	0.00	0.00
Projects	0	0.00	0.00
Field Studies	0	0.00	0.00
Midterm exams	0	0.00	0.00
Others	14	5.00	70.00
Final Exams	1	13.00	13.00
Total Work Load			195.00
Total work load/ 30 hr			6.50
ECTS Credit of the Course			5.00

22	Textbooks, References and/or Other Materials:	[1] Rational Points on Elliptic Curves, J. H. Silverman ve J. Tate, [2]The Arithmetic of Elliptic Curves, J. H. Silverman, [3]Elliptic Curves, L. C. Washington. [4] Introduction to Elliptic Curves and Modular Forms, N. Koblitz.

23	Assesment

TERM LEARNING ACTIVITIES	NUMBER	WEIGHT
Midterm Exam	0	0.00
Quiz	0	0.00
Home work-project	0	0.00
Final Exam	1	100.00
Total	1	100.00
Contribution of Term (Year) Learning Activities to Success Grade		0.00
Contribution of Final Exam to Success Grade		100.00
Total		100.00
Measurement and Evaluation Techniques Used in the Course		

24	ECTS / WORK LOAD TABLE

25	CONTRIBUTION OF LEARNING OUTCOMES TO PROGRAMME QUALIFICATIONS															
	PQ1	PQ2	PQ3	PQ4	PQ5	PQ6	PQ7	PQ8	PQ9	PQ10	PQ11	PQ12	PQ13	PQ14	PQ15	PQ16
ÖK1	5	5	5	5	5	5	5	5	5	5	0	0	0	0	0	0
ÖK2	5	5	5	5	5	5	5	5	5	5	0	0	0	0	0	0
ÖK3	5	5	5	5	5	5	5	5	5	5	0	0	0	0	0	0
ÖK4	5	5	5	5	5	5	5	5	5	5	0	0	0	0	0	0
ÖK5	5	5	5	5	5	5	5	5	5	5	0	0	0	0	0	0
ÖK6	5	5	5	5	5	5	5	5	5	5	0	0	0	0	0	0
ÖK7	5	5	5	5	5	5	5	5	5	5	0	0	0	0	0	0

LO: Learning Objectives PQ: Program Qualifications

Contribution Level:	1 very low	2 low	3 Medium	4 High	5 Very High