

## REAL ANALYSIS II

|      |   |  |
|------|---|--|
| 1    | Course Title:   | REAL ANALYSIS II   |
| 2    | Course Code:  | MAT5102  |
| 3    | Type of Course:   | Optional   |
| 4    | Level of Course:  | Second Cycle   |
| 5    | Year of Study:  | 1  |
| 6    | Semester:   | 2  |
| 7    | ECTS Credits Allocated:   | 6.00   |
| 8    | Theoretical (hour/week):  | 3.00   |
| 9    | Practice (hour/week):   | 0.00   |
| 10   | Laboratory (hour/week):   | 0  |
| 11   | Prerequisites:  | none   |
| 12   | Language:   | Turkish  |
| 13   | Mode of Delivery:   | Face to face   |
| 14   | Course Coordinator:   | Prof. Dr. OSMAN BİZİM  |
| 15   | Course Lecturers:   | Prof. Dr. Osman Bizim  |
| 16   | Contact information of the Course Coordinator:                          | Uludağ Üniversitesi, Fen-Edebiyat Fakültesi<br>Matematik Bölümü, Görükle Bursa-TÜRKİYE 0 224 294 17 57 /<br>obizim@uludag.edu.tr                                 |
| 17   | Website:  |  |
| 18   | Objective of the Course:  | The aim of this course is to review student's undergraduate analysis courses and to correct the deficiencies. So students can be successful in graduate studies. |
| 19   | Contribution of the Course to Professional Development:                 |  |
| 20   | Learning Outcomes:  |  |
|      | 1   | Learns measure and its applications.   |
|      | 2   | Learns measurable sets, measurable functions and the Lebesgue measure.   |
|      | 3   | Learns the Lebesgue integral and its properties.   |
|      | 4   | Learns $L_p$ -spaces and convex functions.   |
|      | 5   | Learns Hilbert spaces, inner-product spaces and linear functionals.  |
|      | 6   | Learns orthonormal sets and trigonometric series.  |
|      | 7   | Learns the Fourier series of continuous functions.   |
|      | 8   |  |
|      | 9   |  |
|      | 10  |  |
| 21   | Course Content:   |  |
|      | <b>Course Content:</b>  |  |
| Week | Theoretical   | Practice   |
| 1    | Set functions and their properties                                      |  |
| 2    | Measure function, measure space and their properties                    |  |
| 3    | Construction of the Lebesgue and the Borel measure and their properties |  |

| <b>4</b>   | Measurable functions   |  |
|--|--|--|
| <b>5</b>   | Simple functions and their properties                          |  |
| <b>6</b>   | The Lebesgue integral of simple functions and their properties |  |
| <b>7</b>   | The Lebesgue convergence theorem and its applications          |  |
| <b>8</b>   | The integral of complex functions and their properties         |  |
| <b>9</b>   | The Riesz-Fischer theorem and its applications                 |  |
| <b>10</b>  | Lp-spaces and their properties                                 |  |
| <b>11</b>  | Convex functions and their properties                          |  |
| <b>12</b>  | Hilbert spaces inner-product spaces and linear functionals.    |  |
| <b>13</b>  | Orthonormal sets and trigonometric series and their properties |  |
| <b>14</b>  | Banach spaces and the Fourier series of continuous functions.  |  |
| <b>22</b>  | Textbooks, References and/or Other Materials:                  | [1] Principles of Mathematical Analysis, W. Rudin,<br>[2] Real and Complex Analysis, W. Rudin,<br>[3] Real Analysis, H. L. Royden,<br>[4] Introduction to Real Analysis, W. F. Trench. |
| <b>23</b>  | Assessment   |  |
| TERM LEARNING ACTIVITIES   |  | NUMBER   |
| Midterm Exam   |  | 0  |
| Quiz   |  | 0  |
| Home work-project  |  | 0  |
| Final Exam   |  | 1  |
| Total  |  | 1  |
| Contribution of Term (Year) Learning Activities to Success Grade |  | 0.00   |
| Contribution of Final Exam to Success Grade                      |  | 100.00   |
| Total  |  | 100.00   |
| Measurement and Evaluation Techniques Used in the Course         |  |  |
| <b>24</b>  | <b>ECTS / WORK LOAD TABLE</b>                                  |  |

| Activites                  | Number | Duration (hour) | Total Work Load (hour) |
|----------------------------|--------|-----------------|------------------------|
| Theoretical                | 14     | 3.00            | 42.00                  |
| Practicals/Labs            | 0      | 0.00            | 0.00                   |
| Self study and preperation | 14     | 5.00            | 70.00                  |
| Homeworks                  | 0      | 0.00            | 0.00                   |
| Projects                   | 0      | 0.00            | 0.00                   |
| Field Studies              | 0      | 0.00            | 0.00                   |
| Midterm exams              | 0      | 0.00            | 0.00                   |
| Others                     | 14     | 5.00            | 70.00                  |
| Final Exams                | 1      | 43.00           | 43.00                  |
| Total Work Load            |        |                 | 225.00                 |
| Total work load/ 30 hr     |        |                 | 7.50                   |
| ECTS Credit of the Course  |        |                 | 6.00                   |

| 25  | CONTRIBUTION OF LEARNING OUTCOMES TO PROGRAMME QUALIFICATIONS |     |       |     |          |     |        |     |             |      |      |      |      |      |      |      |
|---|---|-----|-------|-----|----------|-----|--------|-----|-------------|------|------|------|------|------|------|------|
|   | PQ1   | PQ2 | PQ3   | PQ4 | PQ5      | PQ6 | PQ7    | PQ8 | PQ9         | PQ10 | PQ11 | PQ12 | PQ13 | PQ14 | PQ15 | PQ16 |
| ÖK1   | 5   | 5   | 5     | 5   | 5        | 5   | 5      | 5   | 5           | 5    | 0    | 0    | 0    | 0    | 0    | 0    |
| ÖK2   | 5   | 5   | 5     | 5   | 5        | 5   | 5      | 5   | 5           | 5    | 0    | 0    | 0    | 0    | 0    | 0    |
| ÖK3   | 5   | 5   | 5     | 5   | 5        | 5   | 5      | 5   | 5           | 5    | 0    | 0    | 0    | 0    | 0    | 0    |
| ÖK4   | 5   | 5   | 5     | 5   | 5        | 5   | 5      | 5   | 5           | 5    | 0    | 0    | 0    | 0    | 0    | 0    |
| ÖK5   | 5   | 5   | 5     | 5   | 5        | 5   | 5      | 5   | 5           | 5    | 0    | 0    | 0    | 0    | 0    | 0    |
| ÖK6   | 5   | 5   | 5     | 5   | 5        | 5   | 5      | 5   | 5           | 5    | 0    | 0    | 0    | 0    | 0    | 0    |
| ÖK7   | 5   | 5   | 5     | 5   | 5        | 5   | 5      | 5   | 5           | 5    | 0    | 0    | 0    | 0    | 0    | 0    |
| LO: Learning Objectives    PQ: Program Qualifications |   |     |       |     |          |     |        |     |             |      |      |      |      |      |      |      |
| Contribution Level:                                   | 1 very low  |     | 2 low |     | 3 Medium |     | 4 High |     | 5 Very High |      |      |      |      |      |      |      |