

# NUMBER THEORY I

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| 1    | Course Title:  | NUMBER THEORY I  |  |
| 2    | Course Code:   | MAT5203  |  |
| 3    | Type of Course:  | Optional   |  |
| 4    | Level of Course:   | Second Cycle   |  |
| 5    | Year of Study:   | 1  |  |
| 6    | Semester:  | 1  |  |
| 7    | ECTS Credits Allocated:                                    | 6.00   |  |
| 8    | Theoretical (hour/week):                                   | 3.00   |  |
| 9    | Practice (hour/week):                                      | 0.00   |  |
| 10   | Laboratory (hour/week):                                    | 0  |  |
| 11   | Prerequisites:   | None   |  |
| 12   | Language:  | Turkish  |  |
| 13   | Mode of Delivery:  | Face to face   |  |
| 14   | Course Coordinator:  | Prof. Dr. İSMAİL NACİ CANGÜL   |  |
| 15   | Course Lecturers:  | Prof.Dr.İsmail Naci CANGÜL<br>Prof.Dr.Osman BİZİM  |  |
| 16   | Contact information of the Course Coordinator:             | Uludağ Üniversitesi, Fen-Edebiyat Fakültesi<br>Matematik Bölümü, 16059 Görükle Bursa-TÜRKİYE 0 224 294 17 51<br>tekcan@uludag.edu.tr |  |
| 17   | Website:   |  |  |
| 18   | Objective of the Course:                                   | The aim of the course is to make the students gain the some algebraic properties on number theory                                    |  |
| 19   | Contribution of the Course to Professional Development:    |  |  |
| 20   | Learning Outcomes:   |  |  |
|      |  | 1  | Learn the some fundamental concepts on number theory.  |
|      |  | 2  | Learn the finite fields and algebra on these fields.   |
|      |  | 3  | Learn the Legendre symbol and the relationship between quadratic congruencies and Legendre symbol. |
|      |  | 4  | Learn the Gauss sums and some properties of this sum.  |
|      |  | 5  | Learn the find the simple continued fraction expansion of rational and irrational numbers.         |
|      |  | 6  |  |
|      |  | 7  |  |
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| 21   | Course Content:  |  |  |
|      |  | <b>Course Content:</b>   |  |
| Week | Theoretical  | Practice   |  |
| 1    | Overview of basic concepts on lessons                      |  |  |
| 2    | Algebraic numbers, algebraic groups and reduction theorems |  |  |
| 3    | Finite fields and algebraic operations on them             |  |  |

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| 4  | Prime numbers and the number of prime numbers   |  |
| 5  | Legendre symbol and the relationship between quadratic congruencies and Legendre symbol |  |
| 6  | Ring of Gauss integers  |  |
| 7  | Gauss primes, Galois groups and sums  |  |
| 8  | Rings and units of rings  |  |
| 9  | The relationship between units of rings and the integer solutions of Pell equations     |  |
| 10 | Farey sequences   |  |
| 11 | Quadratic forms and their relationship between the groups $GL(2,Z)$ and $SL(2,Z)$       |  |
| 12 | Positive definite and indefinite quadratic forms  |  |
| 13 | Minkowski theorem and its application   |  |
| 14 | The ring $Z[\exp(2\pi i/n)]$  |  |

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| 22 | Textbooks, References and/or Other Materials: | [1] J. Buchmann and U. Vollmer. Binary Quadratic Forms: An Algorithmic Approach. Springer-Verlag, Berlin, Heidelberg, 2007.<br>[2] D.A. Buell. Binary Quadratic Forms, Classical Theory and Modern Computations. Springer-Verlag, New York, 1989.<br>[3] H.M. Edwards. Fermat's Last Theorem: A Genetic Introduction to Algebraic Number Theory. Graduate Texts in Mathematics, Springer-Verlag, New York, London, Tokyo, 1996.<br>[6] R.A. Mollin. Fundamental Number Theory with Applications. Springer-Verlag, New York, London, Tokyo, 1997. |
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| Activites   |   | Number | Duration (hour) | Total Work Load (hour) |
|---|---|--------|-----------------|------------------------|
| Theoretical   |   | 14     | 3.00            | 42.00                  |
| Practicals/Labs   |   | 0      | 0.00            | 0.00                   |
| Self study and preparation                                      |   | 14     | 7.00            | 98.00                  |
| 22 Assessment   |   |        |                 |                        |
| Homeworks   |   | 0      | 0.00            | 0.00                   |
| Projects  | R | 14     | 5.00            | 70.00                  |
| Field Studies   |   | 0      | 0.00            | 0.00                   |
| Quiz  |   | 0      | 0.00            | 0.00                   |
| Midterm exams   | 0 | 0.00   | 0.00            | 0.00                   |
| Others  |   | 0      | 0.00            | 0.00                   |
| Final Exams   | 1 | 10.00  | 15.00           | 15.00                  |
| Total Work Load   |   |        |                 | 225.00                 |
| Contribution of 100 (Year) Learning Activities to Success Grade |   | 0.00   |                 | 7.50                   |
| ECTS Credit of the Course                                       |   |        |                 | 6.00                   |
| Contribution of Final Exam to Success Grade                     |   | 100.00 |                 |                        |
| Total   |   | 100.00 |                 |                        |
| Measurement and Evaluation Techniques Used in the Course        |   |        |                 |                        |

**24 ECTS / WORK LOAD TABLE**

| 25  | CONTRIBUTION OF LEARNING OUTCOMES TO PROGRAMME QUALIFICATIONS |     |     |     |     |     |     |     |     |      |      |      |      |      |      |      |
|-----|---|-----|-----|-----|-----|-----|-----|-----|-----|------|------|------|------|------|------|------|
|     | PQ1   | PQ2 | PQ3 | PQ4 | PQ5 | PQ6 | PQ7 | PQ8 | PQ9 | PQ10 | PQ11 | PQ12 | PQ13 | PQ14 | PQ15 | PQ16 |
| ÖK1 | 5   | 4   | 2   | 4   | 3   | 3   | 5   | 5   | 5   | 3    | 0    | 0    | 0    | 0    | 0    | 0    |
| ÖK2 | 4   | 3   | 2   | 4   | 3   | 2   | 5   | 5   | 4   | 4    | 0    | 0    | 0    | 0    | 0    | 0    |

|  |                   |   |   |              |   |   |                 |   |   |               |   |   |                    |   |   |   |
|--|-------------------|---|---|--------------|---|---|-----------------|---|---|---------------|---|---|--------------------|---|---|---|
| <b>ÖK3</b>   | 5                 | 4 | 2 | 4            | 4 | 4 | 4               | 5 | 5 | 4             | 0 | 0 | 0                  | 0 | 0 | 0 |
| <b>ÖK4</b>   | 4                 | 3 | 2 | 4            | 3 | 2 | 5               | 5 | 4 | 3             | 0 | 0 | 0                  | 0 | 0 | 0 |
| <b>ÖK5</b>   | 5                 | 3 | 2 | 4            | 3 | 5 | 4               | 5 | 5 | 3             | 0 | 0 | 0                  | 0 | 0 | 0 |
| <b>LO: Learning Objectives    PQ: Program Qualifications</b> |                   |   |   |              |   |   |                 |   |   |               |   |   |                    |   |   |   |
| <b>Contribution Level:</b>                                   | <b>1 very low</b> |   |   | <b>2 low</b> |   |   | <b>3 Medium</b> |   |   | <b>4 High</b> |   |   | <b>5 Very High</b> |   |   |   |